# An Updated Evaluation of the Fe-Gd (Iron-Gadolinium) System

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## **Equilibrium Diagram**

Figure 1 shows the assessed equilibrium diagram that is taken mainly on the calculated diagram based on thermodynamic modeling by [95Liu], but includes consideration of the experimental work of [69Sav] and the evaluated diagram of [82Kub]. The equilibrium phases include: (1) the liquid, L; (2) four peritectic intermetallic compounds, that is, Fe<sub>17</sub>Gd<sub>2</sub>, Fe<sub>23</sub>Gd<sub>6</sub>, Fe<sub>3</sub>Gd, and Fe<sub>2</sub>Gd; and (3) five terminal solid solutions: ( $\alpha$ Fe), ( $\gamma$ Fe), ( $\delta$ Fe), ( $\alpha$ Gd), and ( $\beta$ Gd). Table 1 presents the threephase equilibria and pure metal transformation data. In this evaluation, more comprehensive literature sources were collected. In particular, some pertinent thermodynamic data were found. The liquidus composition at the peritectic equilibrium with Fe<sub>2</sub>Gd is ~20 at.% more Gd-rich than the diagram in [Massalski2]. This result is consistent with the review of [96Oka].

The binary phase diagram of the Fe-Gd system has been investigated by several investigators [60Vic, 61Nov, 61Sav, 62Cop, 64Bur, 69Sav]. [82Kub] proposed an Fe-Gd phase diagram based on [62Cop] with some modifications. Recently, [93Oka] evaluated this system. [61Nov] suggested that seven intermet-

Table 1 Special Folities of the Assessed Fe-Gu Flase Diagram	Table 1	Special Points of the	Assessed Fe-Gd Phase	Diagram
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Reaction		Composition, at.% Fe		Temperature, °C	Reaction type	Reference
$L \leftrightarrow \delta Fe$		100		1538	Melting	[Massalski2]
$\delta Fe \leftrightarrow \gamma Fe$		100		1394	Allotropic	[Massalski2]
$\gamma Fe \leftrightarrow \alpha Fe$		100		912	Allotropic	[Massalski2]
$\delta Fe \leftrightarrow L + \gamma Fe$	~99.4	91	~99.45	1380	Metatectic	[69Sav, 95Liu]
$\gamma Fe + Fe_{17}Gd_2 \leftrightarrow \alpha Fe$	~99.97	89.5	~99.87	~924	Peritectoid	[69Sav, 82Kub, 95Liu]
$\beta Fe_{17}Gd_2 \leftrightarrow \alpha Fe_{17}Gd_2$		89.5		1215	Polymorphic	[90Ati2]
$L + \gamma Fe \leftrightarrow Fe_{17}Gd_2$	88.1	~99.1	89.5	1331	Peritectic	[82Kub, 95Liu]
$L + Fe_{17}Gd_2 \leftrightarrow Fe_{23}Gd_6$	76.6	89.5	79.3	1283	Peritectic	[69Sav, 82Kub, 95Liu]
$L + Fe_{23}Gd_6 \leftrightarrow Fe_3Gd$	52.3	79.3	75	1156	Peritectic	[95Liu]
$L + Fe_3Gd \leftrightarrow Fe_2Gd$	44	75	66.7	1082	Peritectic	[69Sav, 82Kub]
$L \leftrightarrow Fe_2Gd + \alpha Gd$	~26.4	66.7	~0	~832	Eutectic	[69Sav, 95Liu]
$L \leftrightarrow \beta Gd$		0		1313	Melting	[Massalski2]
$\beta Gd \leftrightarrow \alpha Gd$		0		1235	Allotropic	[Massalski2]

#### Table 2 Crystal Structure Data

Phase	Composition, at.% Fe	Pearson symbol	Space group	Strukturbericht designation	Prototype	Reference
(αGd)	0	hP2	P63/mmc	A3	Mg	[61Nov, 71Bru]
(βGd)	0	<i>cI</i> 2	Im3m	A2	W	[71Bru]
Fe2Gd	66.7	cF24	$Fd\overline{3}m$	C15	Cu <sub>2</sub> Mg	[64Man, 78Cre]
Fe3Gd	75	hR12	R3m		Be <sub>3</sub> Nb	[65Smi, 85Sei]
Fe23Gd6	79.3	cF116	Fm3m	$D8_a$	Mn <sub>23</sub> Th <sub>6</sub>	[65Kri]
αFe17Gd2	89.5	hR19	R3m		$Zn_{17}Th_2$	[63Kri, 70Giv]
βFe17Gd2	89.5	hP38	$P6_3/mmc$		Ni <sub>17</sub> Th <sub>2</sub>	[63Kri, 70Giv]
(αFe)	100	<i>cI</i> 2	Im3m	A2	W	[Massalski2]
(γFe)	100	cF4	Fm3m	A1	Cu	[Massalski2]
(δFe)	100	<i>cI</i> 2	Im3m	A2	W	[Massalski2]
Questionable phases						
Fe3Gd2	60		<i>c</i> *30			[61Nov]
Fe7Gd2	77.8		<i>o</i> *18			[61Nov]
Fe4Gd	80	hP10				[61Nov]
Fe5Gd	83.3	hP6	P6/mmm	$D2_d$	CaCu <sub>5</sub>	[60Nas, 61Nov]





#### **Section II: Phase Diagram Evaluations**

allic compounds ( $Fe_3Gd_2$ ,  $Fe_2Gd$ ,  $Fe_3Gd$ ,  $Fe_7Gd_2$ ,  $Fe_4Gd$ ,  $Fe_5Gd$ , and  $Fe_{17}Gd_2$ ) exist, but compounds  $Fe_3Gd_2$ ,  $Fe_7Gd_2$ , and  $Fe_5Gd$  have not been confirmed by other measurements [61Sav, 62Cop, 69Sav]. [61Sav] reported compounds  $Fe_{17}Gd_2$  and  $Fe_2Gd$ , and a third compound, hinted at by thermal analysis. [62Cop] confirmed the existence of the compounds  $Fe_9Gd$ ,  $Fe_3Gd$ , and  $Fe_2Gd$ . The compound  $Fe_0Gd$  may be inferred as

Fe<sub>17</sub>Gd<sub>2</sub>. According to [Shunk], the phase diagram of [64Bur] included four compounds: Fe<sub>17</sub>Gd<sub>2</sub>, Fe<sub>4</sub>Gd, FeGd, and FeGd<sub>2</sub>. The last two compounds are unusual. [64Bur] probably mistook Fe<sub>3</sub>Gd and Fe<sub>2</sub>Gd for FeGd and FeGd<sub>2</sub>, respectively [93Oka], because Fe<sub>3</sub>Gd and Fe<sub>2</sub>Gd occur in the phase diagram of [69Sav] (same research group). [69Sav] showed Fe<sub>17</sub>Gd<sub>2</sub> and Fe<sub>2</sub>Gd as certain with Fe<sub>4</sub>Gd and Fe<sub>3</sub>Gd as ques-

 Table 3
 Fe-Gd Lattice Parameter Data

	Composition,	La	attice parameters, nm		D.f.
Phase	at.% Fe	a	b	С	Reference
αGd	0	0.3635		0.5780	[61Nov, 71Bru]
		0.36336		0.5781	[Massalski2]
βGd	0	0.406			[71Bru]
Fe <sub>2</sub> Gd	66.78	0.7450			[44End]
		0.7400			[60Nas]
		0.7530			[61Nov]
		0.7390			[60Wer, 62Cop, 68Ray, 87Ich]
		0.7389			[61Bae]
		0.7360			[61Sav]
		0.7355			[64Man]
		0.740			[78Cre]
		0.73909			[68Man]
		07394			[72Can_62Hub]
		0.73875			[74Atz]
		0.7396			[70Bus]
		0.7390			[70Dus]
		0.7403			[02Klc]
E. C.I	75	0.7390	•••		
Fe3Od	15	0.5205		1.505	[611N0V]
		0.5148	•••	2.402	
		0.51692		2.4737	[66 van]
		0.51654		2.4707	[68Dw1]
		0.5166		2.471	[68Ray]
		0.5157		2.470	[85Sei]
Fe <sub>23</sub> Gd <sub>6</sub>	79.3	1.2134			[65Kri]
		1.212			[86Nag]
$\beta Fe_{17}Gd_2$	89.5	0.839		0.853	[61Nov]
		0.850		0.835	[63Kri]
		0.8486		0.8349	[66Bus]
		0.8496		0.8345	[70Giv]
$\alpha Fe_{17}Gd_2$	89.5	0.8536		1.2429	[61Kri, 61Sav]
		0.855		1.240	[63Kri]
		0.8517		1.2429	[66Bus]
		0.8538		1.2431	[68Ray]
		0.8540		1.2428	[70Giv]
αFe	100	0.28665			[Massalski2]
γFe	100	0.36467			[Massalski2]
δFe	100	0.29315			[Massalski2]
Questionable phases					
Fe3Gd	60	0.825			[61Nov]
FerGd2	77.8	0.571	0.678	0.715	[61Nov]
Fe4Gd	80	0.515		0.664	[61Nov]
Fe5Gd	83.3	0.50		0.41	[61Nov]
		0.492		0.411	[61Nov]
		0.483		0.413	[62Hub]
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tionable. In line with the other Fe-RE systems, the earlier reported  $Fe_4Gd$  was written as  $Fe_{23}Gd_6$  [Moffatt, 82Kub]. The Fe-Gd binary phase diagram was thermodynamically assessed by [95Liu] and is similar to that given by [82Kub] and [93Oka] with four peritectic intermetallic compounds:  $Fe_{17}Gd_2$ ,  $Fe_{23}Gd_6$ ,  $Fe_{3}Gd$ , and  $Fe_{2}Gd$ , and one eutectic reaction.

#### **Terminal Phases**

The Gd dissolves less than 0.6 at.% Fe [62Cop]. The transformation temperature for  $\alpha \leftrightarrow \beta$  is 1235 °C [Massalski2]. However, the alternative reports were 1260 °C [82Kub], 1261 °C [63Hul], and 1284 °C [71Bru]. The melting point of Gd was suggested to be 1313 °C by [Massalski2], 1312 °C by [71Bru], and 1315 °C by [63Hul]. The data from [Massalski2] are commonly accepted.

[95Liu] reported 1239 °C as the  $\beta$ Gd  $\leftrightarrow \alpha$ Gd + L reaction temperature according to his thermodynamic assessment using the data of [91Din] for pure elements. Because there is no experimental data to confirm this reaction, it is not adopted in Fig. 1.

The  $\delta Fe \leftrightarrow L + \gamma Fe$  invariant reaction is at 1380 °C [69Sav, 82Kub, 95Liu], and the compositions of the phases are from [95Liu].

#### Fe<sub>2</sub>Gd

This compound was obtained independently by [60Wer], [61Nov], and [78Cre]. It is formed by a peritectic reaction at 1080 °C. The liquidus composition at the peritectic melting of Fe<sub>2</sub>Gd is ~56 at.% Gd [95Liu] or ~59 at.% Gd [69Sav], which differs by ~20 at.% from that given by [62Cop], [82Kub], and [93Oka]. In view of the systematic trends of the Fe-RE systems, the diagram of [69Sav] and [95Liu] appears to be more reasonable [96Oka]. The value of [95Liu] is adopted in Fig. 1.

The L  $\leftrightarrow$  Fe<sub>2</sub>Gd + ( $\alpha$ Gd) eutectic is reported at 830 °C, 72 at.% Gd [61Sav, 69Sav]; at 845 °C, 66.9 at.% Gd [62Cop]; at 845 °C, 70 at.% Gd [82Kub]; at 849 °C, 72 at.% Gd [64Bur]; or at 832 °C, 73.6 at.% Gd [95Liu].

#### Fe<sub>3</sub>Gd

The existence of the compound Fe<sub>3</sub>Gd was first confirmed by [61Nov] and [62Cop] using thermal, x-ray, and metallographic

methods. Fe<sub>3</sub>Gd melts peritectically at 1156 °C with the liquidus composition of ~44 at.% Gd [95Liu] or at 1155 °C with the liquidus composition of ~34 at.% Gd [82Kub, 93Oka]; the former value is adopted in Fig. 1.

#### Fe<sub>23</sub>Gd<sub>6</sub>

The earlier reported  $Fe_4Gd$  [59Nes, 61Nov] should probably be written as  $Fe_{23}Gd_6$  with  $Mn_{23}Th_6$ -type structure [65Kri, 77Bus]. [84Her], [86Nag], and [90Ati1] confirmed the existence of  $Fe_{23}Gd_6$ . It is likely formed peritectically at 1280 °C [82Kub], but only very slowly [84Her]. The formation of the compound is accelerated by using less pure starting materials, with O as one effective impurity. [93Oka] suggested that  $Fe_{23}Gd_6$  may be stable only in a restricted temperature range immediately below the melting point at 1280 °C, whereas other investigators found  $Fe_{23}Gd_6$  to be a stable phase at room temperature [92Tia] and at 500 °C [95Zhu].

#### Fe<sub>17</sub>Gd<sub>2</sub>

This compound melts peritectically at 1331°C [67Liu]. Fe<sub>17</sub>Gd<sub>2</sub> is currently accepted as crystallizing in two modifications: a high-temperature phase with the hexagonal Ni<sub>17</sub>Th<sub>2</sub>-type structure and a low-temperature phase with rhombohedral Zn<sub>17</sub>Th<sub>2</sub>-type structure with the polymorphic transition temperature being 1215 °C [90Ati2]. Neglecting

# Table 4Experimental Enthalpies of Mixing in theFe-Gd System at 1850 K

Composition,	
at.% Gd	$-\Delta H_{\rm f},$ kJ/mol
0	0
10	$1.25\pm0.14$
20	$3.09\pm0.34$
30	$4.93\pm0.71$
40	$6.37\pm0.91$
50	$7.21\pm0.83$
60	$7.36\pm0.62$
70	$6.82\pm0.42$
80	$5.66 \pm 0.29$
90	$3.64\pm0.20$
100	0

Table 5	Experimental	<b>Enthalpies of Fo</b>	ormation in the	Fe-Gd System
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Compound	Δ <i>H</i> <sub>f</sub> , kJ/mol	<i>Т</i> , К	Method	Temperature of experiment, K	Reference
Fe <sub>2</sub> Gd	-11.6 -3.5	298 1078	solution calorimetry in liquid Al reaction calorimetry	998 	[86Col] [75Deo]
Fe <sub>3</sub> Gd Fe <sub>17</sub> Gd <sub>2</sub>	-9.3 -2.3	298 298	solution calorimetry in liquid Al solution calorimetry in liquid Al	988 1092	[87Col1] [87Col1]

#### Table 6 Measured $T_c$ and $\beta$ Values Used in the Assessed Fe-Gd System

Phase	Fe <sub>2</sub> Gd	Fe <sub>3</sub> Gd	Fe <sub>23</sub> Gd <sub>6</sub>	Fe <sub>17</sub> Gd <sub>2</sub>
<i>T</i> <sub>c</sub> , K	782	728	468	472
β, μ <sub>B</sub>	3.35	1.6	14.8	21.2

Liquid	$L_{\rm Fe,Gd}^{0,\rm L} = -27\ 625 + 17.869T$
	$L_{\rm Fe,Gd}^{1,\rm L} = 14\ 594 - 8.894T$
bcc	$L_{\rm Fe,Gd}^{0,\rm bcc} = -28\ 758 + 38.096T$
fcc	$L_{\rm Fe,Gd}^{0,{\rm fcc}} = 30\ 231$
cph	$L_{\rm Fe,Gd}^{0,{\rm cph}} = 1\ 000\ 000$
Fe <sub>17</sub> Gd <sub>2</sub>	$G_{\text{Ferdd}}^{0,\text{Fe}}$ $G_2^{\text{Gd}} - 17G_{\text{Fe}}^{0,\text{hecc}} - 2G_{\text{Gd}}^{0,\text{heph}} = -218\ 222 + 98.884T$
Fe <sub>23</sub> Gd <sub>6</sub>	$G_{\text{Ee},\text{Gd}}^{0,\text{Fe}_{23}}$ Gd $-23G_{\text{Fe}}^{0,\text{hbcc}} - 6G_{\text{Gd}}^{0,\text{hcph}} = -430\ 075 + 182.333T$
Fe3Gd	$G_{\text{FerGd}}^{0,\text{Fe}Gd} - 3G_{\text{Fe}}^{0,\text{hecc}} - G_{\text{Gd}}^{0,\text{hech}} = -61\ 393 + 26.214T$
Fe <sub>2</sub> Gd	$G_{\text{Fe:Gd}}^{0,\text{Fe},\text{Gd}} - 2G_{\text{Fe}}^{0,\text{hecc}} - G_{\text{Gd}}^{0,\text{hecph}} = -46\ 829 + 63.295T - 5.917T\ \ln T - 353\ 121T^{-1} - 94\ 463\ 542T^{-3}$

 Table 7
 Thermodynamic Parameters Obtained by [95Liu] (in SI units)

 Table 8
 Curie Temperature Values in the Fe-Gd System

Phase	Composition, at.% Fe	Tc, K	Reference
Fe2Gd	66.7	782	[64Man]
		788	[74Dar]
		796	[77Bus]
		810	[85Zho]
Fe3Gd	75.0	729	[77Bus]
Fe23Gd6	79.3	659	[77Bus]
Fe <sub>17</sub> Gd <sub>2</sub>	89.5	476	[77Bus]

ranges of homogeneity is common when calculating phase diagrams because such neglect greatly simplifies the calculating procedure, and the diagram in Fig. 1 is based primarily on the calculated diagram of [95Liu]. There is strong evidence for a range of homogeneity for Fe<sub>17</sub>Gd<sub>2</sub>. Indeed, [81Sta] has reported that the Zn<sub>17</sub>Th<sub>2</sub>-type structure occurs only for Fe-deficient stoichiometries, Fe<sub>17-r</sub>Th<sub>2</sub>. Further, a range of homogeneity for the phase was reported by [66Bus] who found the rhombohedral Zn<sub>17</sub>Th<sub>2</sub>-type structure for annealed alloys across a range of compositions. [66Bus] also found that quenched stoichiometric alloys had the Ni<sub>17</sub>Th<sub>2</sub>type structure while quenched alloys through the composition range Fe17Gd2 and Fe7Gd showed both the rhombohedral Zn<sub>17</sub>Th<sub>2</sub>-type structure and the hexagonal Ni<sub>17</sub>Th<sub>2</sub>-type structure. Finally, in quenched alloys near a stoichiometry of Fe<sub>7</sub>Gd, [66Bus] found weak reflections from Fe<sub>3</sub>Gd mixed with reflections from the Zn<sub>17</sub>Th<sub>2</sub>-type structure. Later work by [70Giv] showed that alloys near the composition Fe<sub>7</sub>Gd could be indexed on hexagonal lattice parameters of a = 0.4905 to 0.4931 nm and c = 0.4173 to 0.4143 nm, which are characteristic of the closely related CaCu<sub>5</sub>-type structure. [70Giv] postulated that such a diffraction pattern could be produced by the substitution of one Gd atom by two Fe atoms (2 to 1 is approximately the atom volume ratio of Gd to Fe) on a significant number of Gd crystallographic sites. Thus there is definite evidence for a range of homogeneity, but composition limits for the homogeneity range await determination.

### **Metastable Phases**

Many compounds reported by early authors [61Nov, 61Gsc, 66Bus] were not confirmed by later investigations. There is the possibility that some of those unconfirmed compounds are metastable phases. Further, there is still a question as to what portion of the reports of [66Bus, 70Giv, 77Bus] represents equilibrium and what represents transient kinetic effects or metastability.

#### **Formation of Amorphous Phases**

The ability to form amorphous alloys can be estimated by the imaginary eutectic that is obtained from extrapolation of the terminal liquidus lines of each element. In the Fe-Gd system, the formation range of the amorphous phase shifts from the real eutectic composition (about 70 at.% Gd) toward the virtual eutectic composition (about 50 to 60 at.% Gd). The atomic size effect of constituent elements on the metallic glass formation was discussed by introducing the atomic volume mismatch evaluated from the cube of the atomic radius of solvent and solute [85Uen]. Amorphous Fe-Gd alloys, ribbons about 15 µm thick, from 16 to 70 at.% Gd, were prepared with a meltquenching method in a vacuum [91Tok]. Samples from 16 to 70 at.% Gd were obtained by [91Yan]. The αGd phase appeared in these samples at higher Gd concentrations. In addition, pure Gd, Fe, and  $Fe_{1-r}Gd_r$  thin films were thermally evaporated with a thickness of 500 to 700 Å [84Lee1, 84Lee2]. The composition dependence of the as-deposited material showed three different regions: (1) an amorphous alloy and  $\alpha$ Fe mixture up to 24 at.% Gd, (2) an amorphous alloy phase in the composition range from 24 to 60 at.% Gd, and (3) a Gd and an amorphous alloy mixture above 60 at.% Gd.

#### **Thermal Stabilities of Amorphous Films**

Amorphous alloys are in a nonequilibrium state and crystallize to lose their amorphous characteristics above a certain temperature. Several relevant investigations have been carried out on the Fe-Gd alloy system. The results of thermomagnetization [91Yan] showed three types of crystallization processes: (1)  $\alpha$ Fe, Fe<sub>23</sub>Gd<sub>6</sub>, and Fe<sub>2</sub>Gd at the composition 22 at.% Gd, (2)  $\alpha$ Fe, Fe<sub>2</sub>Gd, and  $\alpha$ Gd in the region 33.3 to 58 at.% Gd, and (3) Fe<sub>2</sub>Gd and  $\alpha$ Gd at the composition 70 at.% Gd. The XRD study [91Tok] indicated that these amorphous alloys crystallized into two phases,  $\alpha$ Gd and the Laves phase (Fe<sub>2</sub>Gd) without any trace of the  $\alpha$ Fe phase. In addition, the investigation of the crystallization process for amorphous thin films by means of in situ transmission electron microscopy [84Lee1, 84Lee2] was characterized by the three reaction stages: (1)  $\alpha$ Fe and  $\alpha$ Gd were precipitated by primary crystallization, (2) some transient intermetallic compounds were formed, and (3) the equilibrium phases were formed by subsequent decomposition reactions. During the in situ crystallization reaction, the  $\alpha$ Fe phase appeared in the first or the second but not the final reaction stage.

The onset temperatures of crystallization are different among different investigations because of different heating times and cooling rates. [91Yan] reported that crystallization did not start below the Curie temperature of any amorphous alloy. This result is in accordance with that of x-ray measurement [91Tok] but different from that for bulk ribbon (60 at.% Gd) obtained by [79Bus] who reported that  $\alpha$ Gd began to precipitate around 140 °C.

#### **Magnetic Properties of Amorphous Alloy Films**

The evaporated amorphous film of Fe-Gd was reported to possess a perpendicular anisotropy sufficient to cause the magnetization to be normal to the film plane [74Hei], particularly in the vicinity of the magnetic compensation point\* [78Mim]. The mean field model [75Hei, 76Hei] was proposed to calculate a systematic variation of the Curie temperature associated with a variation of composition and rare earth species and also to reproduce the observed shape of magnetization-versus-temperature curves. [78Mim], [84Lee1], and [91Yan] investigated the Curie temperature,  $T_{\rm comp}$ , for amorphous Fe-Gd alloys at different compositions.

### Crystal Structures and Lattice Parameters

Crystal structure and lattice parameter data for the phases in the Fe-Gd system are summarized in Tables 2 and 3.

#### Thermodynamics

The specific heat anomaly of Fe<sub>2</sub>Gd, a singularity in the heat capacity around the magnetic ordering temperature, was measured and discussed by [74Dar]. The lower temperature specific heat was determined in the temperature range 8 to 300 K [81Ger1]. The crystal field contribution to the heat capacity was evaluated [81Ger2]. The Gd<sup>3+</sup> is an *s*-state ion and as such is not expected to interact with the crystalline electric field. However, [81Ger2] illustrated that this contribution was significant. The heat capacity of Fe<sub>2</sub>Gd intermetallic compound over the temperature region 1.5 to 10 K was also measured [79But]. Values for the apparent electronic heat capacity between 5 and 10 K were determined as  $C_p = \Gamma'T + T^3\beta$  with coefficients  $\Gamma' = 19.3$  mJ/mole-K<sup>2</sup>, and  $\beta = 0.296$  mJ/mole-K<sup>4</sup>.

A molecular field model for analytically predicting entropy change in the temperature region  $T \ge T_c$  was developed for the Fe-Gd system at the composition 89.5 at.% Fe [84Oes]. Enthalpies of mixing for liquid alloys were measured at 1850 K by [89Nik] (Table 4). The enthalpies of formation of transition rare earth metal alloys were collected by [87Col2]; these include values for Fe<sub>2</sub>Gd, Fe<sub>3</sub>Gd, and Fe<sub>17</sub>Gd<sub>2</sub> compounds (Table 5). The phase relations and thermodynamic data of the Fe-Gd system were thermodynamically assessed by [95Liu].

For some phases, there is a magnetic transformation. According to [78Hil], the magnetic contribution to the Gibbs energy,  $G_m^{\text{mg},\phi}$ , in the structure  $\phi$  is described by:

$$G_{\rm m}^{{\rm mg},\varphi} = RT \ln (\beta^{\varphi} + 1) f(\tau)$$

$$\tau = T/T_c^{\varphi} \tag{Eq 1}$$

where  $T_c^{\varphi}$  is the critical (Curie or Neel) temperature and  $\beta^{\varphi}$  the magnetic moment,  $f(\tau)$  are the polynomials generated by [78Hil].  $T_c$  and  $\beta$  are taken from the measured critical temperature and the mean Bohr magnetic moment per mole. Table 6 lists the values of  $T_c$  and  $\beta$  used by [95Liu].

# Thermodynamic Models of Liquid, fcc, bcc, and cph Phases

The liquid, fcc, bcc, and cph phases are treated by a one-sublattice model for which the Gibbs energy expression is:

$$G_{\rm m}^{\phi} = X_{\rm Fe} G_{\rm Fe}^{0,\phi} + X_{\rm Gd} G_{\rm Gd}^{\phi} + RT(X_{\rm Fe} \ln X_{\rm Fe} + X_{\rm Gd} \ln X_{\rm Gd}) + G_{\rm m}^{mg,\phi} + X_{\rm Fe} X_{\rm Gd} \sum_{i} L_{\rm Fe,Gd}^{i,\phi} (X_{\rm Fe} - X_{\rm Gd})^{i}$$
(Eq 2)

where  $X_i$  is the mole fraction of element i (i = Fe, Gd),  $G_i^{0,\phi}$  is the molar Gibbs energy in the structure  $\varphi$  in nonmagnetic states,  $L_{\text{Fe},\text{Gd}}^{i,\varphi}$  are the binary interaction parameters, and  $G_m^{mg,\varphi}$  is the magnetic contribution to the Gibbs energy.

#### Thermodynamic Models of Intermetallic Compounds

All the intermetallic compounds are treated as stoichiometric phases. Their Gibbs energies per mole of formula unit  $\text{Fe}_A\text{Gd}_B$  can be expressed as:

$$G_{\rm m}^{0, \operatorname{Fe}_A \operatorname{Gd}_B} = A \ G_{\operatorname{Fe}}^{0, \operatorname{hbcc}} + B \ G_{\operatorname{Gd}}^{0, \operatorname{hcph}} + a + bT + cT \ln T$$
$$+ G_{\rm m}^{0, \operatorname{mg}, \operatorname{Fe}_A \operatorname{Gd}_B} \tag{Eq 3}$$

where  $G_{Gd}^{0,hcph}$  and  $G_{Fe}^{0,hbcc}$  are the Gibbs energies of the respective pure elements in a hypothetical nonmagnetic cph and bcc structure, and  $G_m^{0,mg,Fe_AGd_B}$  is the magnetic contribution to the Gibbs energy.

<sup>\*</sup> The ferromagnetic coupling of Fe when in combination with heavy rare earth elements such as Gd causes a decrease in the spontaneous magnetization,  $M_s$ , with increasing temperature, whereas the antiferromagnetic coupling of Gd causes an increase in the spontaneous magnetization with increasing temperature. The temperature at which the increase due to Gd matches the decrease due to Fe is known as the compensation temperature.

#### Section II: Phase Diagram Evaluations

The thermodynamic data for pure elements are from the work of [91Din] with reference to SER (standard element reference) at 298.15 K.

A consistent thermodynamic description of this system obtained by [95Liu] is given in Table 7. The calculated phase equilibria agree well with the literature data [61Sav, 69Sav].

# Magnetism

The magnetic properties of the intermediate phases have been investigated in various laboratories [71Kir, 74Kli, 74Dar, 64Man, 59Nes, 81Ger]. [77Bus] has compiled the magnetic data for various rare earth/transition metal compounds and lists mean values. [85Zho] studied the magnetic properties of Fe<sub>2</sub>Gd. The Curie temperatures of the compounds in the Fe-Gd system are given in Table 8.

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\*Indicates key paper. #Indicates presence of a phase diagram.

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